

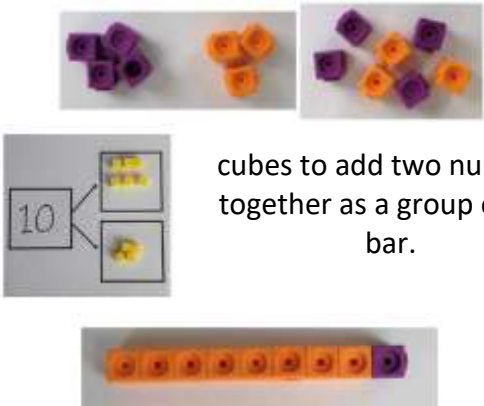
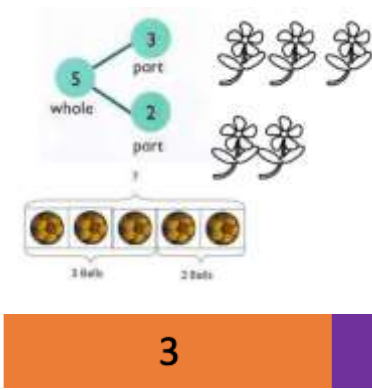
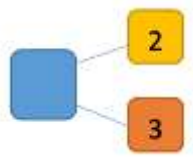
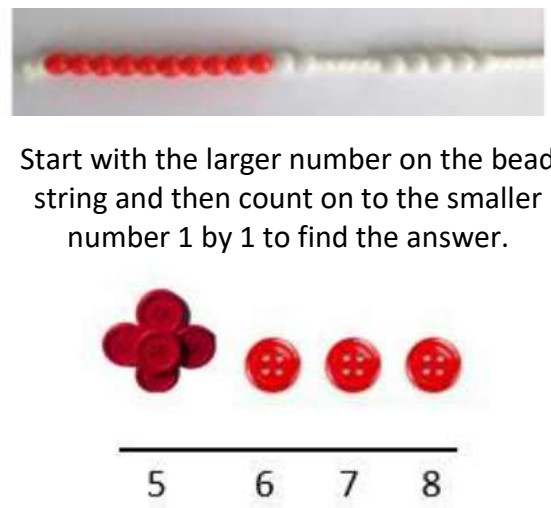


PROGRESSION THROUGH CALCULATION GUIDANCE

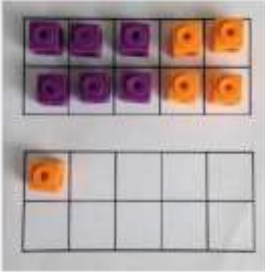
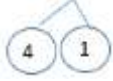


This guidance has been developed from the White Rose Calculation Policy: working document, which was written as a guide to indicate the progression through Addition, Subtraction, Multiplication and Division in Years 1 – 6.

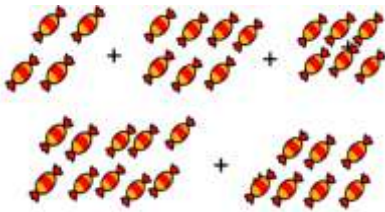
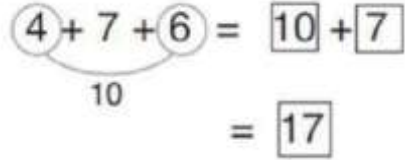
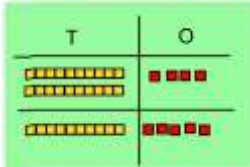
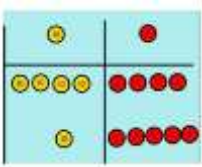
Calculation Guidance: Addition

	Objective	Concrete	Pictorial	Abstract
Year 1	Number bonds of 5, 6, 7, 8, 9 and 10	 Use the cubes to add two numbers together as a group or in a bar.	 Use pictures to add two number together as a group or in a bar.	$2 + 3 = 5$ $3 + 2 = 5$ $5 = 3 + 2$ $5 = 2 + 3$  Use the part-part-whole diagram as shown above to move into the abstract.
	Counting	 Start with the larger number on the bead string and then count on to the smaller number 1 by 1 to find the answer.	 Use a number line to count on in ones.	$5 + 3 = 8$

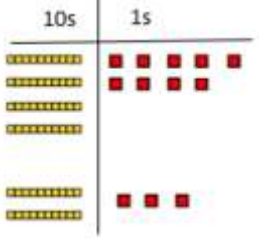
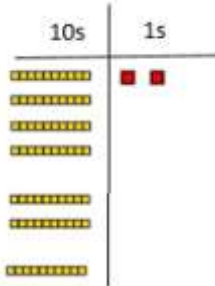
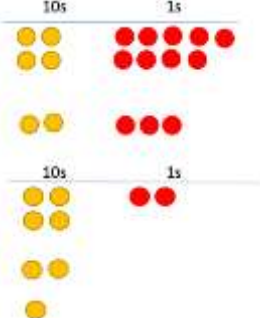
Calculation Guidance: Addition

	Regrouping to make 10	  $6 + 5 = 11$ Start with the bigger number and use the smaller number to make 10.	 $6 + 5 = 11$  $6 + 4 = 10$ $10 + 1 = 11$	$6 + 5 = 11$
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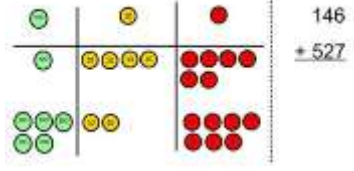
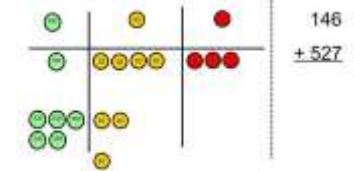
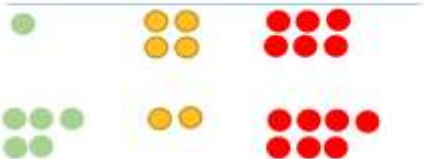
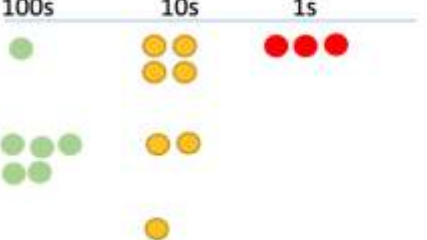
Calculation Guidance: Addition

	Objective	Concrete	Pictorial	Abstract
Year 2	Adding 3 single digit numbers	$4 + 7 + 6 = 17$ Put 4 and 6 together to make 10. Add on 7.  Following on from making 10, make 10 with 2 of the digits (if possible) then add on the third digit.	 Add together three groups of objects. Draw a picture to recombine the groups to make 10.	 Combine the two numbers that make 10 and then add on the remainder.
	Column method without regrouping	Add together the ones first, then add the tens. Use the Base 10 blocks first before moving onto place value counters. $24 + 15 =$  $44 + 15 =$ 	After physically using the base 10 blocks and place value counters, children can draw the counters to help them to solve additions. $10s$  $1s$ 	$24 + 15 = 39$ $\begin{array}{r} 24 \\ +15 \\ \hline 39 \end{array}$

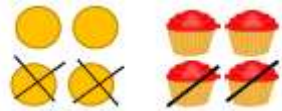
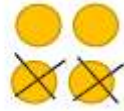
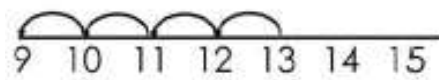
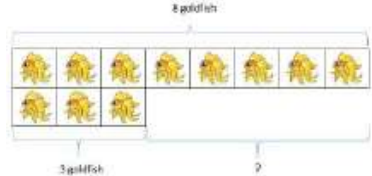
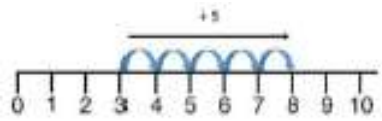
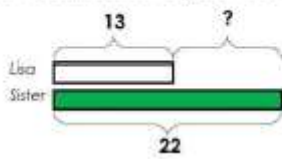
Calculation Guidance: Addition

	Column method with regrouping	Make both numbers on the place value grid.  Add up the units and exchange 10 ones for 1 ten. 	Using place value counters, children can draw the counters to help them to solve additions. 	$49 + 23 = 72$ $40 + 9$ <u>$20 + 3$</u> $60 + 12 = 72$
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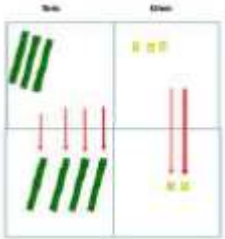
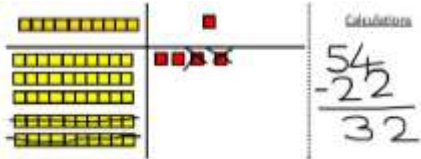
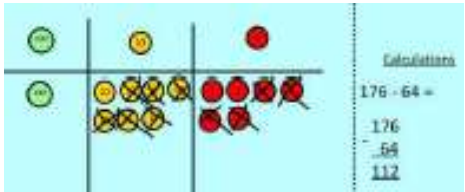
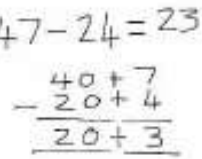
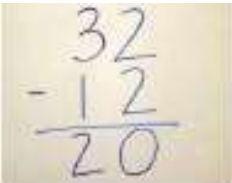
Calculation Guidance: Addition

	Objective	Concrete	Pictorial	Abstract
Year 3/4	Column method with regrouping.	Make both numbers on a place value grid.  Add up the units and exchange 10 ones for 1 ten.  As children move on to decimals, money and decimal place value counters can be used to support learning. NB By Year 4, children will progress on to adding four-digit numbers.	100s 10s 1s  100s 10s 1s  Children can draw a pictorial representation of the columns and place value counters to further support their learning and understanding. NB Addition of money needs to have £ and p added separately.	$146 + 527 = 673$ $100 + 40 + 6$ $\underline{500 + 20 + 7}$ $600 + 70 + 3 = 673$
Year 5/6	Column method with regrouping.	Consolidate understanding by using numbers with more than 4 digits and extend by adding numbers with up to 3 decimal places.		

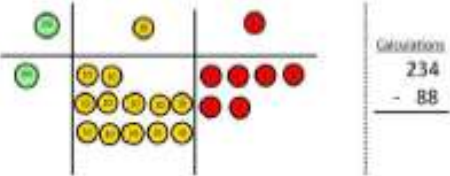
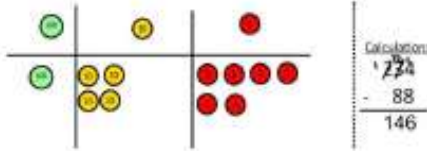
Calculation Guidance: Subtraction

	Objective	Concrete	Pictorial	Abstract
Year 1	Taking away ones.	Use physical objects, counters, cubes etc. to show how objects can be taken away. $4 - 2 = 2$ 	Cross out drawn objects to show what has been taken away. $4 - 2 = 2$ 	$4 - 2 = 2$
	Counting back.	Make the larger number in your subtraction. Move the beads along your bead string as you count backwards in ones.  $13 - 4 = 9$	Count back on a number line or number track.  Start at the bigger number and count back the smaller number, showing the jumps on the number line.	Put 13 in your head, count back 4. What number are you at? Use your fingers to help.
	Find the difference.	Compare amounts and objects to find the difference.  Use cubes to build towers or make bars to find the difference. Use basic bar models with items to find the difference.	 Count on to find the difference. <i>Lisa is 13 years old. Her sister is 22 years old. Find the difference in age between them.</i>  Draw bars to find the difference between two numbers.	Hannah has 8 goldfish. Helen has 3 goldfish. Find the difference between the number of goldfish the girls have.

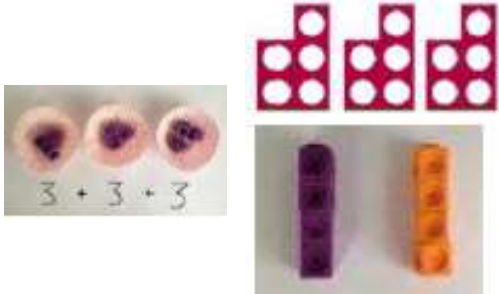
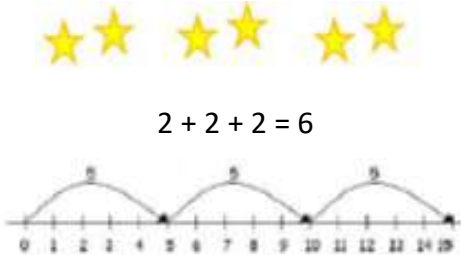
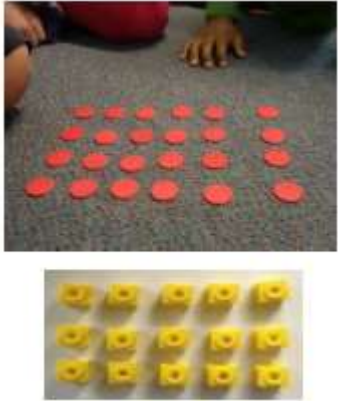
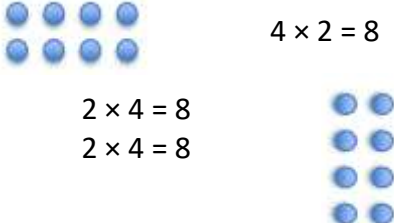
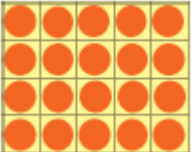
Calculation Guidance: Subtraction

	Objective	Concrete	Pictorial	Abstract
Year 2	Column method without regrouping.	75 - 42 = 33  Use Base 10 to make the bigger number then take the smaller number away. Show how you partition numbers to subtract.  Again, make the larger number first.	 Draw the Base 10 or place value counters alongside the written calculation to help to show working. 	47 - 24 = 23  This will lead to a clear written column subtraction. 

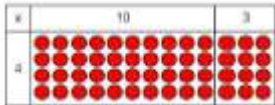
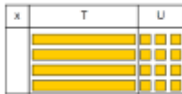
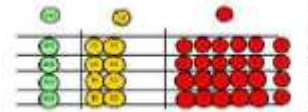
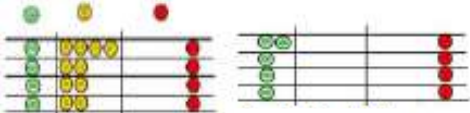
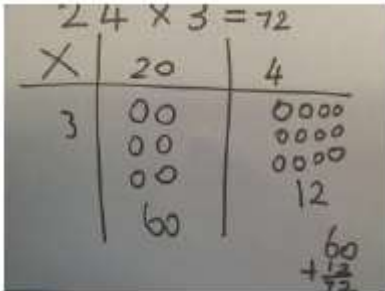
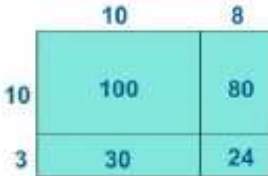
Calculation Guidance: Subtraction

	Objective	Concrete	Pictorial	Abstract
Year 3/4/5/6	Column method with regrouping.	Now look at the tens, can I take away 8 tens easily? I need to exchange 1 hundred for 10 tens.  Now I can take away 8 tens and complete my subtraction.  Show children how the concrete method links to the written method alongside your working. Cross out the numbers when exchanging and show where we write our new amount.		

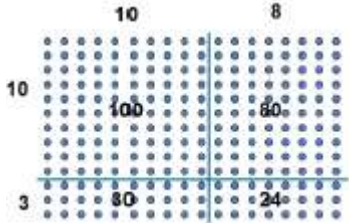
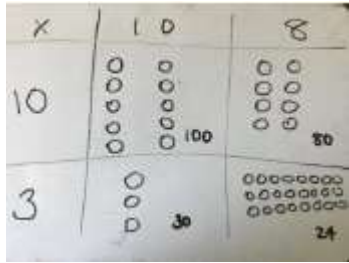
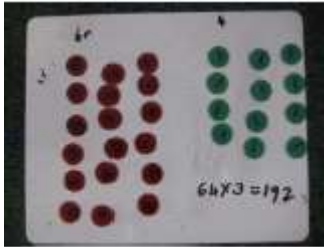
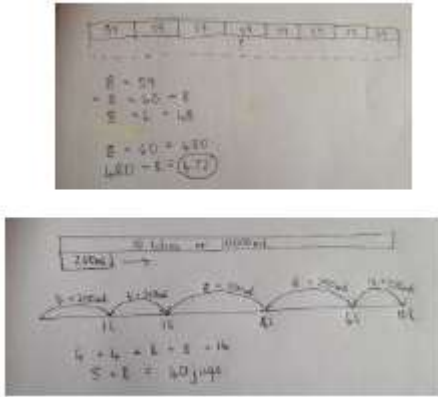
Calculation Guidance: Multiplication

	Objective	Concrete	Pictorial	Abstract
Year 1/2	Repeated addition.	Use different objects to add equal groups. 	There are 3 plates. Each plate has 2 star biscuits on. How many biscuits are there?  $2 + 2 + 2 = 6$ $5 + 5 + 5 = 15$	Write addition sentences to describe objects and pictures.  $2 + 2 + 2 = 6$
	Arrays – showing commutative multiplication	Create arrays using counters/cubes to show multiplication sentences. 	Draw arrays in different rotations to find commutative multiplication sentences.  $4 \times 2 = 8$ $2 \times 4 = 8$ $2 \times 4 = 8$ $4 \times 2 = 8$ Link arrays to area of rectangles. 	Use an array to write multiplication sentences and reinforce repeated addition.  $5 + 5 + 5 = 15$ $3 + 3 + 3 + 3 + 3 = 15$ $5 \times 3 = 15$ $3 \times 5 = 15$

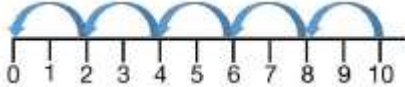
Calculation Guidance: Multiplication

	Objective	Concrete	Pictorial	Abstract																					
Year 3/4	Grid method	Show the link with arrays to first introduce the grid method.  4 rows of 10 4 rows of 3 Move on to using Base 10 to move towards a more compact method.  4 rows of 13 Move on to place value counters to show how we are finding groups of a number. We are multiplying by 4 so we need 4 rows.  Fill each row with 126.  Add up each column, starting with the ones making any exchanges needed.  $4 \times 126 = 504$	Children can represent the work they have done with place value counters in a way that they understand. They can draw the counters, using colours to show different amounts or just use circles in the different columns to show their thinking as shown below. 	Start with multiplying by one digit numbers and showing the clear addition alongside the grid. <table><tr><td>X</td><td>30</td><td>5</td></tr><tr><td>7</td><td>210</td><td>35</td></tr></table> $210 + 35 = 245$ Moving forward, multiply by a 2 digit number showing the different rows within the grid method.  <table><tr><td>X</td><td>1000</td><td>300</td><td>40</td><td>2</td></tr><tr><td>10</td><td>10000</td><td>3000</td><td>400</td><td>20</td></tr><tr><td>8</td><td>8000</td><td>2400</td><td>320</td><td>16</td></tr></table>	X	30	5	7	210	35	X	1000	300	40	2	10	10000	3000	400	20	8	8000	2400	320	16
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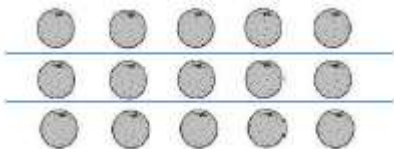
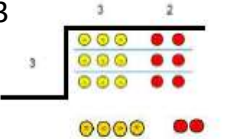
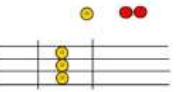
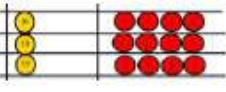
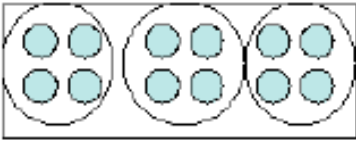
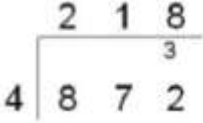
Calculation Guidance: Multiplication

	Expanded method.	Show the link with arrays to first introduce the expanded method. 		Start with long multiplication, reminding the children about lining up their numbers clearly in columns. $\begin{array}{r} 18 \\ \times 13 \\ \hline 24 \text{ (3 x 8)} \\ 30 \text{ (3 x 10)} \\ 80 \text{ (10 x 8)} \\ \hline 234 \end{array}$
Year 5/6	Compact method.	Children can continue to be supported by place value counters at the stage of multiplication.  It is important at this stage that they always multiply the ones first and note down their answer followed by the tens which they note below.	Bar modelling and number lines can support learners when solving problems with multiplication alongside the formal written methods. 	Start with long multiplication, reminding the children about lining up their numbers clearly in columns. $\begin{array}{r} 74 \\ \times 63 \\ \hline 212 \\ 440 \\ \hline 4662 \end{array}$ If it helps, children can write out what they are solving next to their answer. $\begin{array}{r} 1342 \\ \times 18 \\ \hline 13420 \\ 10736 \\ \hline 24156 \end{array}$ This moves to the more compact method.

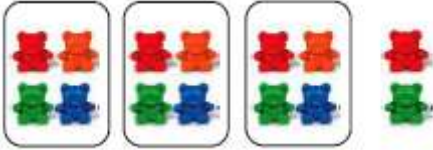
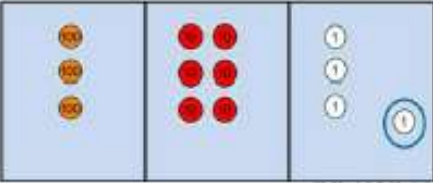
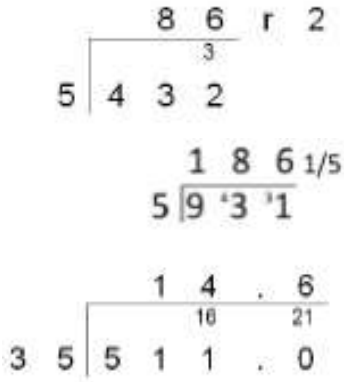
Calculation Guidance: Division

	Objective	Concrete	Pictorial	Abstract
Year 1/2	Sharing.	I have 8 cubes, can you share them equally between two people?	Children use pictures or shapes to share quantities.  $8 \div 2 = 4$	Share 8 buns between two people.  $8 \div 2 = 4$
	Grouping.	Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding.  	Use a number line to show jumps in groups. The number of jumps equals the number of groups.  Think of the bar as a whole. Split it into the number of groups you are dividing by and work out how many would be within each group.  $10 \div 5 = ?$ $5 \times ? = 10$	$10 \div 5 = 2$ Divide 10 into 5 groups. How many are in each group?

Calculation Guidance: Division

	Objective	Concrete	Pictorial	Abstract
Year 3/4	Division with arrays.	Link division to multiplication by creating an array and thinking about the number sentences that can be created. E.g. $15 \div 3 = 5$ $5 \times 3 = 15$ $15 \div 5 = 3$ $3 \times 5 = 15$ 	 Draw an array and use lines to split the array into groups to make multiplication and division sentences.	Find the inverse of multiplication and division sentences by creating four linking number sentences. $5 \times 3 = 15$ $3 \times 5 = 15$ $15 \div 5 = 3$ $15 \div 3 = 5$
	Short division.	Use place value counters to divide using the short division method alongside. $96 \div 3$  $42 \div 3$ Start with the biggest place value. We are sharing 40 into three groups. We can put 1 ten in each group and we have 1 ten left over.  We exchange this ten for 10 ones and then share the ones equally among the groups. We look at how many are in each group. 	Students can continue to use drawn diagrams with dots or circles to help them divide numbers into equal groups.  Encourage them to move towards counting in multiples to divide more efficiently.	Begin with divisions that divide equally with no remainder. 

Calculation Guidance: Division

	Objective	Concrete	Pictorial	Abstract
Year 5/6	Division with remainders.	$14 \div 3 =$ Divide objects between groups and see how much is left over. 	Jump forward in equal jumps on a number line then see how many more you need to jump to find a remainder.  Draw dots and group them to divide an amount and clearly show a remainder. 	Complete written divisions and show the remainder using r. 
	Short division with remainders.	$364 \div 3 =$ 		Move onto divisions with a remainder. Once children understand remainders, begin to express as a fraction or decimal according to the context. 

Calculation Guidance: Division

	Objective	Concrete	Pictorial	Abstract
Year 6	Long division			Children will use long division to divide numbers with up to 4 digits by 2 digit numbers. $ \begin{array}{r} 015 \\ 32 \overline{) 487} \\ \underline{-0} \\ 48 \\ \underline{-32} \\ 167 \\ \underline{-160} \\ 7 \end{array} $ $ \begin{array}{r} 17 \text{ r } 19 \\ 31 \overline{) 546} \\ \underline{31} \downarrow \\ 236 \\ \underline{217} \\ 19 \end{array} $